

Figure 1

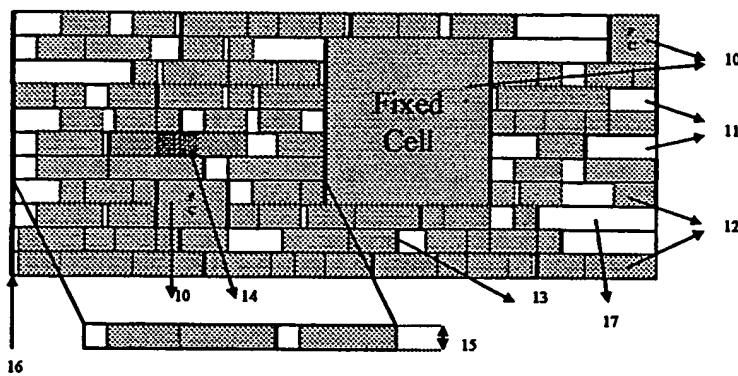


Figure 2

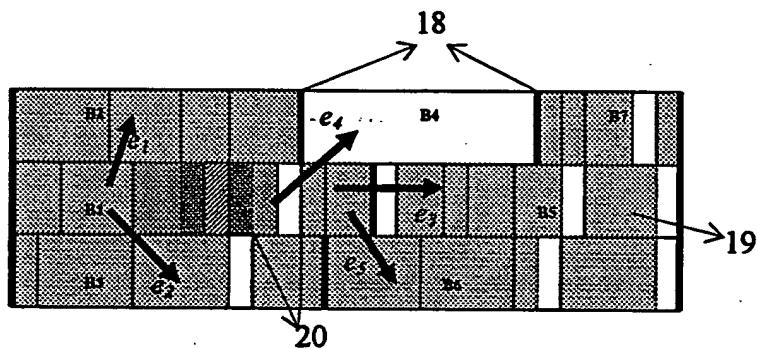
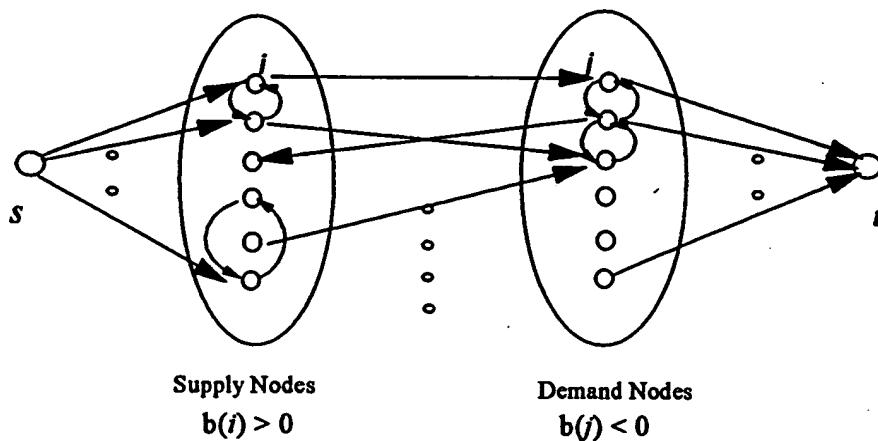


Figure 3


 $\forall i \text{ if } b(i) > 0,$
 $\text{Cap}(e_{si}) = b(i)$
 $\text{Cost}(e_{si}) = 0$
 $\forall i \neq s, j \neq t,$
 $\text{Cap}(e_{ij}) = \text{Infinity (Large Int)}$
 $\text{Cost}(e_{ij}) = K e_{ij}$
 $\forall j \text{ if } b(j) < 0,$
 $\text{Cap}(e_{jt}) = -b(j)$
 $\text{Cost}(e_{jt}) = 0$

\forall : Notation represents the meaning "For Every Element"

\in : Notation represents the meaning "Element of"

Figure 4

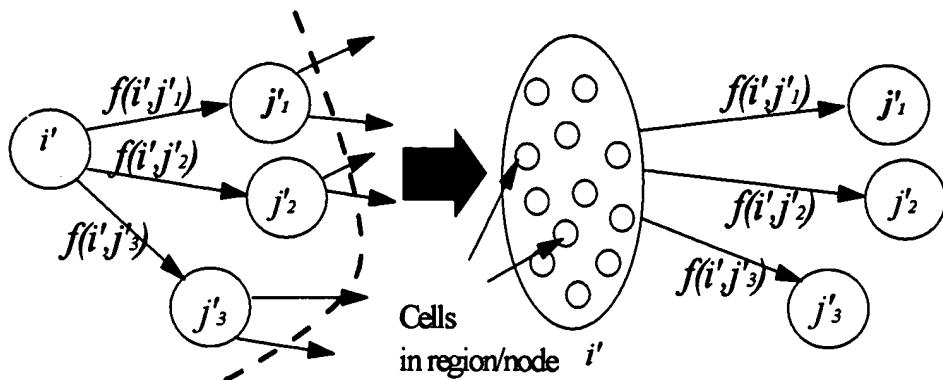
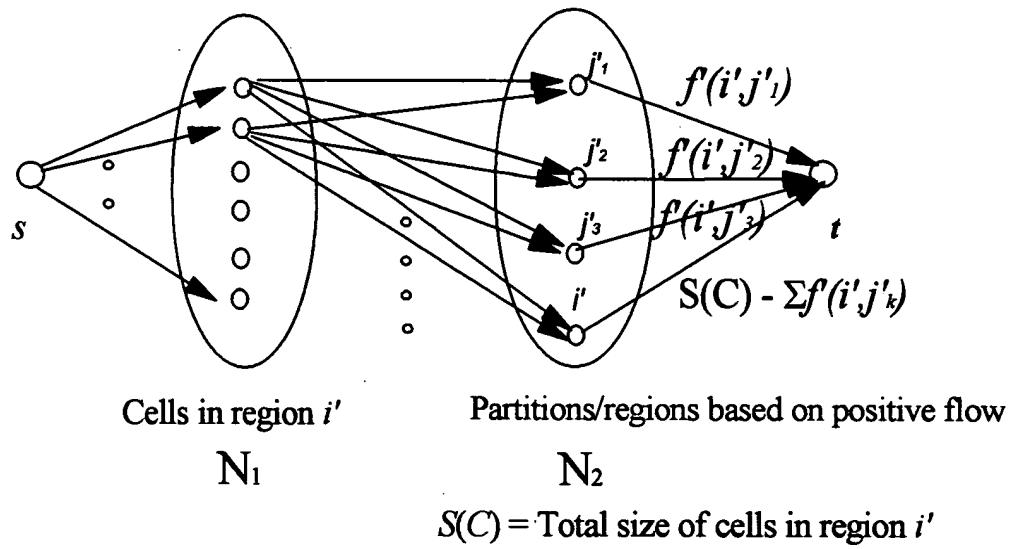


Figure 5



$\forall i \in N_1$
 $\text{Cap}(e_{si}) = 1$
 $\text{Cost}(e_{si}) = 0$

$\forall i \in N_1, j \in N_2,$
 $\text{Cap}(e_{ij}) = 1$
 $\text{Cost}(e_{ij}) = \text{Cost of moving}$
 $\text{cell } i \text{ to region } j$
 $\text{multiplier } \mu_{ij} = \text{size of cell } i$

$\forall j \in N_2$
 $\text{Cap}(e_{jt}) = \text{flow to region } j$
 $\text{Cost}(e_{jt}) = 0$

\forall : Notation represents the meaning "For Every Element"
 \in : Notation represents the meaning "Element of"

Figure 6

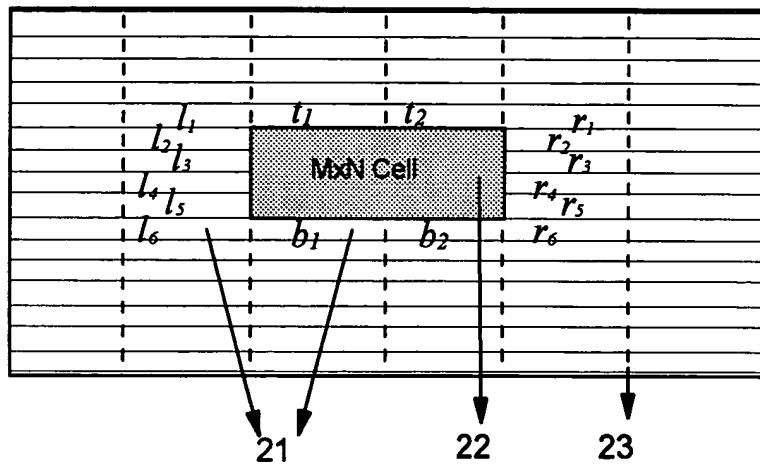
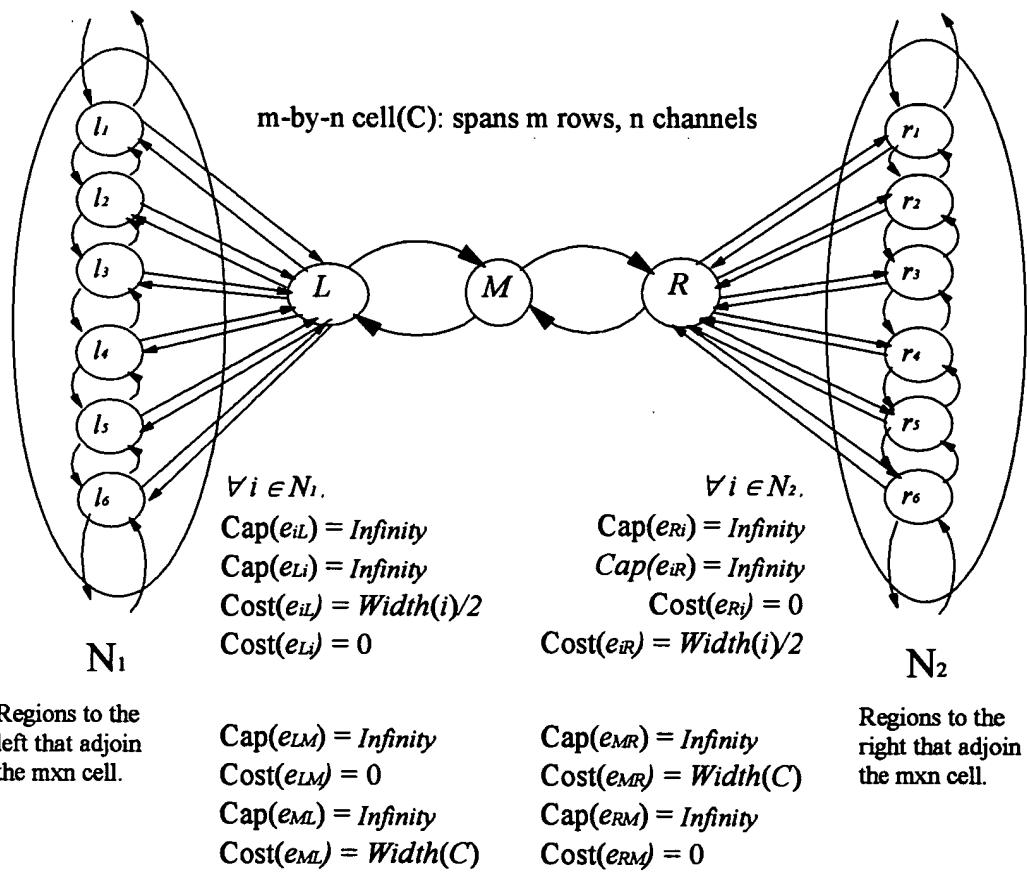


Figure 7



\forall : Notation represents the meaning "For Every Element"

Figure 8

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Placement_Aware_Region_Definition 0
Begin
1 Build placement image
2 For each circuit row  $r$  in the layout
  Begin
    3   scanline_x = row_xlow( $r$ ); last_region_boundary = row_xlow( $r$ );
    4   leading_free_space = false;
    5    $S$  = sorted list of cells in row  $r$  by increasing position along  $x$ -direction
    6    $c$  = first cell in sorted list  $S$ 
    7   while ( $c$ )
      Begin
        8     If ( $xpos(c) > scanline_x$ )
        9       Begin
          10      If ( $xpos(c) - last\_region\_boundary > W$ )
            11        Else
              12          If (is_fixed_cell( $c$ ) || is_blockage( $c$ ) || leading_free_space)
              13             $p$  = create_region ( $r, last\_region\_boundary + W, last\_region\_boundary$ )
              14            scanline_x = (last_region_boundary +  $= W$ )
              15            leading_free_space = false
            16          Else if ( $xpos(c) - scanline_x \geq 0.50 * W$  and  $scanline_x > last\_region\_boundary$ )
              17             $p$  = create_region ( $r, scanline_x, last\_region\_boundary$ )
              18            last_region_boundary = scanline_x
              19            leading_free_space = true
            20          Else
              21            If ( $xpos(c) == scanline_x$ )
              22              Begin
                23                If (is_fixed_cell( $c$ ) || is_blockage( $c$ ))
                24                   $p$  = create_region ( $r, xpos(c) + width(c), scanline_x$ )
                25                  scanline_x += width( $c$ )
                  last_region_boundary = scanline_x
                26              Else if (is_movable_cell( $c$ ))
                27                Begin
                  28                  If ( $xpos(c) + width(c) \leq W$ )
                  29                    scanline_x += width( $c$ )
                  30                  Else
                    31                    Begin
                      32                       $p$  = create_region ( $r, xpos(c) + width(c), last\_region\_boundary$ )
                      last_region_boundary = scanline_x
                      scanline_x += width( $c$ )
                    33                  End
                34              End
              35            End
            36          End
          37        End
        38      End
    39    End
  End
End

```

Figure 9

Global_Area_Migration_Graph ($G(V,E)$)

Begin

1. $V = \{\text{regions}\}$, $E = \{\text{edge between neighboring regions}\}$
2. $\forall e \in E, \text{Cost}(e) = K_e$
3. $\forall e \in E, \text{Cap}(e) = \text{Infinity}$ (Large integer)
4. $\forall v \in V, \text{Size}(v) = \text{Total size of movable cells in } v$
5. $\forall v \in V, \text{Cap}(v) = \text{Total available space for movable cells in } v$ (i.e. region)
6. $\forall v \in V, b(v) = \text{Size}(v) - \text{Cap}(v)$
7. If $b(v) > 0$, v is a supply node.
8. If $b(v) < 0$, v is a demand node.
9. If $b(v) = 0$, v is a transshipment node.

End

\forall : Notation represents the meaning "*For Every Element*"

\in : Notation represents the meaning "*Element of*"

Figure 10

Generalized_Flow_Graph (region i')**Begin**

1. $N_1 = \{\text{cells in region } i'\}, N_2 = \{i'\} \cup \{\text{neighboring regions}\}$
2. $E = \{\text{edge representing cell-to-region assignment}\}$
3. $S(N_1) = \text{Total size of cells in } N_1 \text{ (region } i')$
4. $\text{Smallest}(N_1) = \text{Smallest cell size in } N_1 \text{ (region } i')$
5. *Introduce an edge from N_1 to N_2 for every possible cell-to-region assignment,*
 - $\forall i \in N_1, j \in N_2, \text{Cap}(e_{ij}) = 1$
 - $\forall i \in N_1, j \in N_2, \text{multiplier, } \mu_{ij} = \text{size of cell } i$
 - $\forall i \in N_1, j \in N_2, \text{Cost}(e_{ij}) = \text{Cost of moving cell } i \text{ to region } j$
6. *Introduce source node s , with edges such that*
 - $\forall i \in N_1, \text{Cap}(e_{si}) = 1$
 - $\forall i \in N_1, \text{Cost}(e_{si}) = 0$
7. *Introduce sink node t , with edges such that*
 - $\forall j \in N_2, \text{Cap}(e_{jt}) = f(i', j) = \text{MAX}(\text{Smallest}(N_1), f(i', j)), \text{If } f(i', j) > 0$
 - $0, \text{Otherwise}$

$\forall j \in N_2, \text{Cost}(e_{jt}) = 0$

End \forall : Notation represents the meaning "For every element" \in : Notation represents the meaning "Element of" (a set theory notation)**Figure 11**